

Strategies for Optimised STG Decomposition

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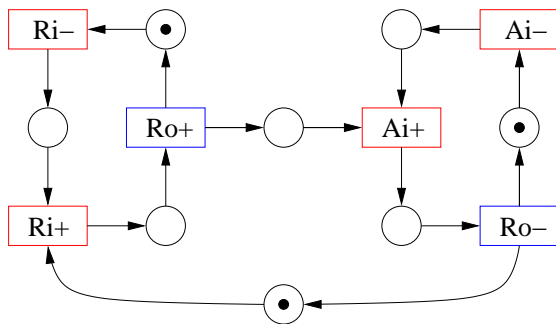
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ACSD 2006

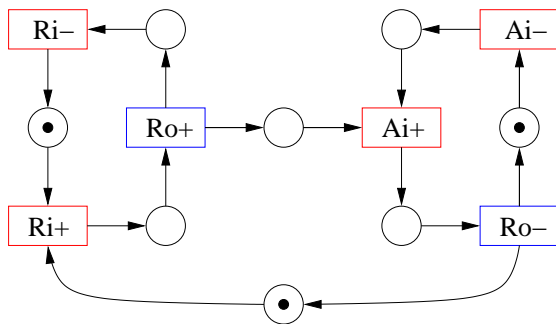
- 1 STG Decomposition
 - STGs
 - Decomposition
- 2 New Decomposition Strategies
 - Contraction Reordering
 - Lazy Backtracking
 - Tree Decomposition
 - Results
- 3 Future Research

- Signal Transition Graphs are Petri nets
- Transitions are labelled with signal edges
- Modell for asynchronous circuits
- Input signal edge activated \rightarrow circuit is ready to receive it from the environment
- Output/internal signal edge activated \rightarrow circuit must produce this signal edge



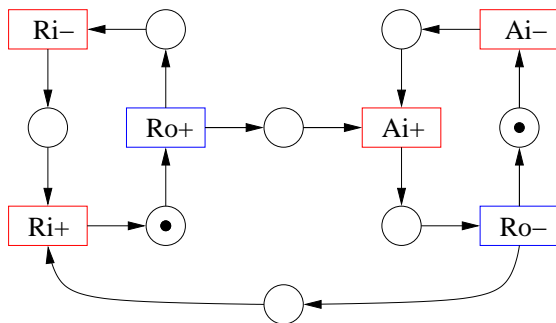
inputs

outputs



inputs

outputs



inputs

outputs

Motivation for Decomposition

- Synthesising a circuit from an STG N
 - Generate the reachability graph R of $N \rightarrow$ state explosion
 - Derive an equation for each output signal from R
 - Effort more than linear in $|R|$
 - Quadratic for the naïve approach
 - Better methods work with BDDs or SAT-solving

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 - Split an STG into components, each producing a subset of outputs
 - Perform synthesis for the components
 - Advantage: Smaller reachability graphs
 - Overall performance improvement

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During decomposition reachability graphs must not be generated!

Decomposition Outline

- For a specification N , choose a partition of the output signals
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 - Includes outputs
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 - Contract λ -labelled transition
 - Delete redundant places and transitions

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 - Contract λ -labelled transition
 - Delete redundant places and transitions
- If necessary, **backtracking**:
 - Go back to initial component
 - **Delambdarise** additional signal
 - Start again

Decomposition Outline

N

Decomposition Outline

$$N \xrightarrow{\lambda} N_0$$

Decomposition Outline

$$N \xRightarrow{\lambda} N_0 \xrightarrow{t_0} N_1$$

Decomposition Outline

$$N \xRightarrow{\lambda} N_0 \xrightarrow{t_0} N_1 \xrightarrow{t_1} N_2$$

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$$N \xRightarrow{\lambda} N_0 \xrightarrow{t_0} N_1 \xrightarrow{t_1} N_2 \xrightarrow{t_2} N_3 \xrightarrow{t_3} \dots N_k \xrightarrow{t_k}$$

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$\Downarrow a = \text{sig}(t_k)$

N'_0

Decomposition Outline

$$\begin{array}{ccccccccccc} N & \xRightarrow{\lambda} & N_0 & \xrightarrow{t_0} & N_1 & \xrightarrow{t_1} & N_2 & \xrightarrow{t_2} & N_3 & \xrightarrow{t_3} & \dots & N_k & \xrightarrow{t_k} \\ & & \Downarrow a = \text{sig}(t_k) & & & & & & & & & & \\ & & N'_0 & \xrightarrow{t'_0} & N'_1 & \xrightarrow{t'_1} & \dots & & & & & & \end{array}$$

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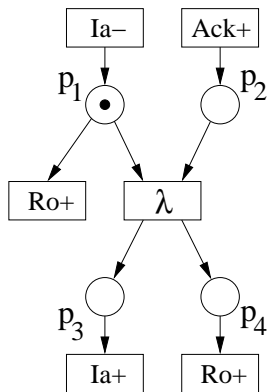
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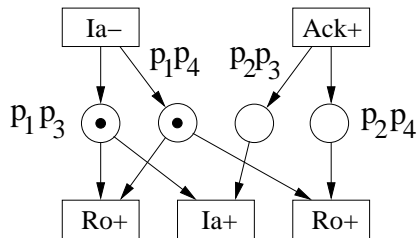
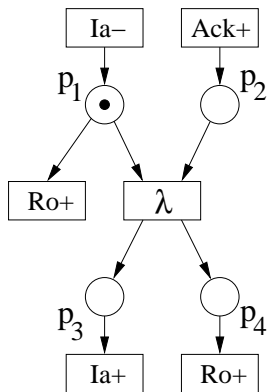
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Transition Contraction

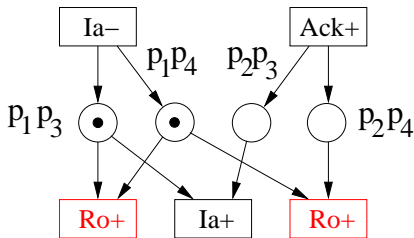
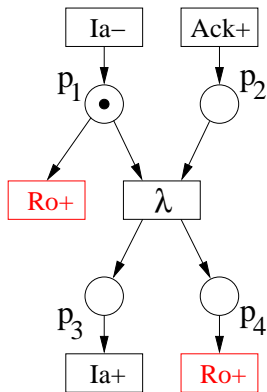


Transition Contraction



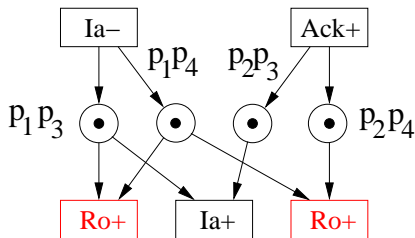
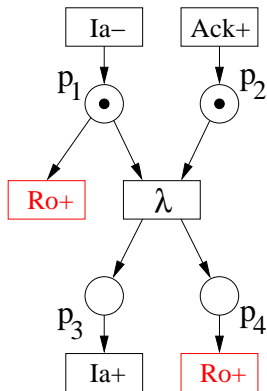
Backtracking is performed if no more λ -transition can be contracted, because the contraction

- ... is not defined (loops, arcweight ≥ 2)
- ... is not-secure (language changed)
- ... generates structural **auto-conflict**



Structural auto-conflict

Auto-Conflicts



Dynamic auto-conflict

New Decomposition Strategies

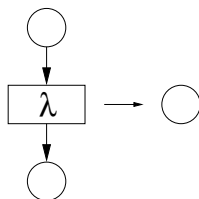
- Contraction reordering
- Lazy backtracking
- Tree decomposition

Contraction Reordering

- Contraction of 'good' transitions produces few new places

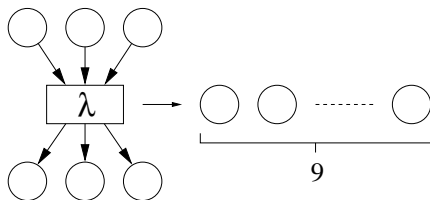
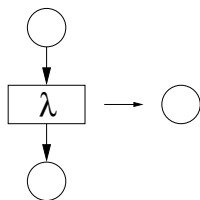
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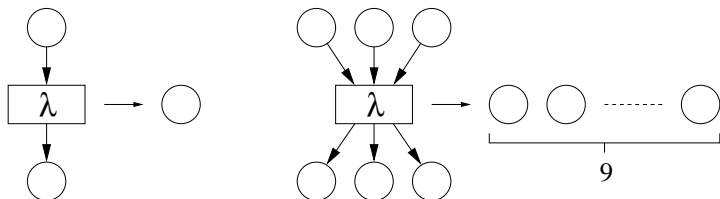
Contraction Reordering

- Contraction of 'good' transitions produces few new places
- Contraction of 'bad' transitions produces many new places



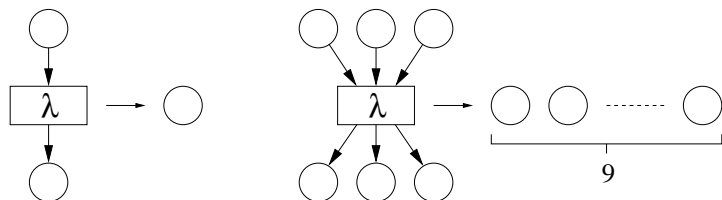
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- Observation: Contracting 'good' transitions first, results in smaller intermediate STGs (important for looking for redundant places)



Contraction Reordering

- Contraction of 'good' transitions produces few new places
- Contraction of 'bad' transitions produces many new places
- Observation: Contracting 'good' transitions first, results in smaller intermediate STGs (important for looking for redundant places)
- Sometimes, contracting 'bad' transitions first results in bigger final STGs
- Therefore, contract 'good' transitions first



Lazy Backtracking

- Contract transitions grouped by former signals
- After a signal was completely contracted save the intermediate result
- When backtracking, don't start at the beginning

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$\downarrow a_j$
 N'_j

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$$\begin{array}{ccc} \dots N_{j-1} & \xrightarrow{a_{j-1}} & N_j \xrightarrow{a_j} \\ \downarrow a_j & & \downarrow a_j \\ N'_{j-1} & & N'_j \end{array}$$

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Tree Decomposition

- Components are generated separately even if they are similar (nearly the same signals should be contracted)
- Tree decomposition:
 - Group contractions by former signals (as for lazy backtracking)
 - Find an appropriate order of contractions
 - Reuse intermediate results

Tree Decomposition

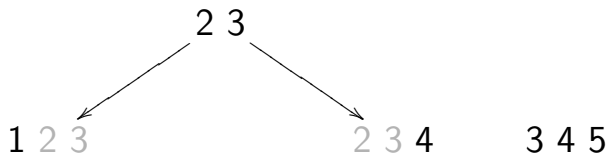
Tree Decomposition

1 2 3

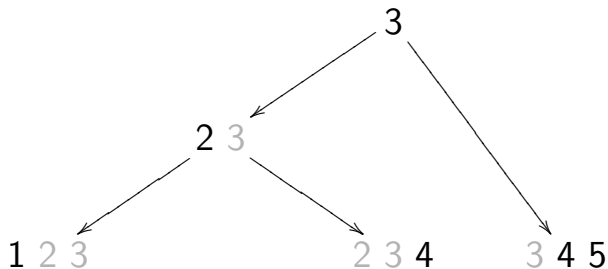
2 3 4

3 4 5

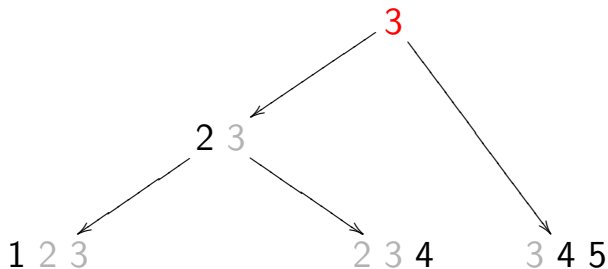
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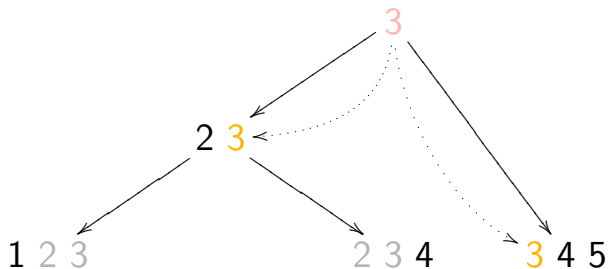
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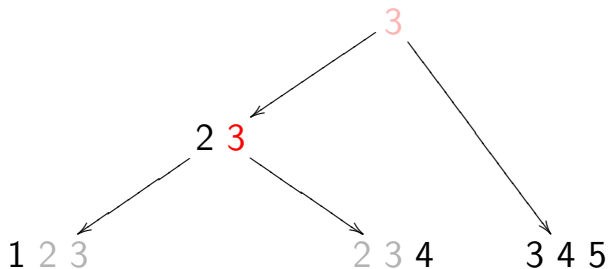
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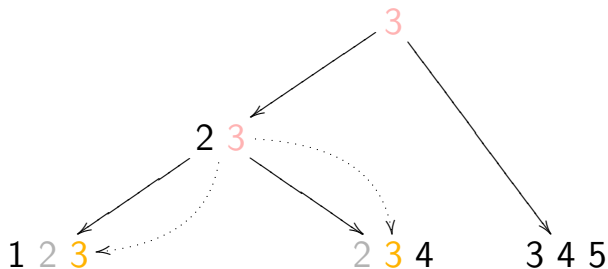
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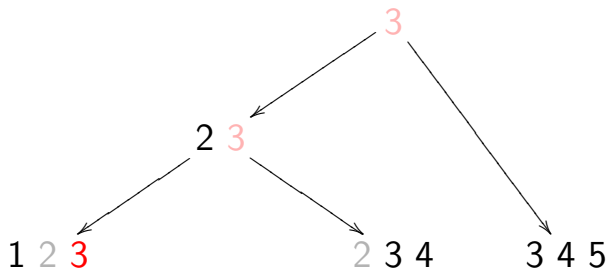
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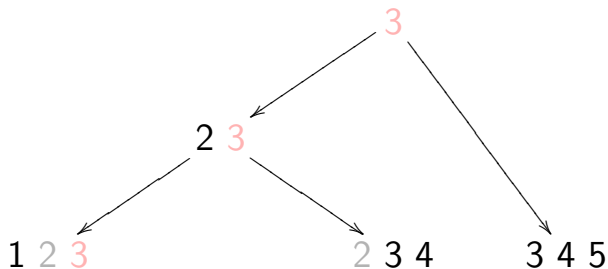
Tree Decomposition



Tree Decomposition



Tree Decomposition



STG	tree		random	
	t (sec)	size	t (sec)	size
2pp.arb.nch.9.csc	2	227	58	4939
2pp.arb.nch.9	2	198	71	2398
2pp.arb.nch.12.csc	6	275	158	3083
3pp.arb.nch.9	4	350	281	13198
3pp.arb.nch.12.csc e	14	537	627	7289
3pp.arb.nch.12	15	422	632	7142

(More results and detailed discussion in the paper)

- In most cases all new strategies perform much better than basic decomposition
- In most cases the components get smaller for every strategy
- Especially tree decomposition reduces runtimes while producing small components

Decomposition is fast enough now → improve the *quality* of the results

- Combine tree decomposition with CSC solving
- Combine decomposition with Handshakecircuits, e.g. generated by Balsa