

References Relating to Reasoning about Partial Functions

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Abstract

This note lists references which address –in some way or another– the problems relating to formal manipulation of logical expressions where terms can fail to denote.

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